

8. Find  $\frac{d}{dx} \left( \ln \left( \frac{2+x}{2-x} \right) \right)$  and hence  $\int \frac{1}{4-x^2} dx$
9. Find  $\frac{d}{dx} \ln (\cos x)$  and hence  $\int_0^{\frac{\pi}{3}} \tan x \, dx$

## • AREA AND VOLUME

1.

- Write down the formula for the area bounded between the curve  $y = f(x)$  and lines  $x = a$  and  $x = b$
- Write down the formula for the area bounded between the curve  $x = g(y)$  and lines  $y = c$  and  $y = d$
- Write down the area bounded between the 2 curves  $y = f(x)$  and  $y = g(x)$  if the curves intersect at  $x = a$  and  $x = b$
- Write down the formula for the volume generated when the area under the curve  $y = f(x)$  between  $x = a$  and  $x = b$  is revolved about the  $x$  axis.
- Write down the formula for the volume generated when the area between the curve  $y = f(x)$  and the  $y$  axis is revolved about the  $y$  axis.

2. For the following questions write down how you would evaluate the areas of the regions without performing the integration. However, a sketch is required.

- Find the area of the region bounded by the curve  $f(x) = x^2 - 9x + 14$ , the  $x$  axis and the ordinates  $x = 3$  and  $x = 6$
- Find the area of the region bounded by the curve  $f(x) = x^2 - 6x$  the  $x$  axis and the ordinates  $x = 2$  and  $x = 8$
- Find the area of the region bounded by the  $x$  axis, the curve  $f(x) = (2x + 1)^2$  the line  $y = 8x$  given that their point of intersection is  $(\frac{1}{2}, 4)$
- Find the points where the line  $y = 3x - 4$  intersects the parabola  $y = x^2 - 3x - 4$  and find the exact area bounded by the line and the parabola.
- Find the area enclosed by the arc of the curve  $x = y^2 - y$  and the  $y$  axis.
- Find the area enclosed between the curve  $y = \sqrt{x}$ , the  $y$  axis and the line  $y = 4$
- Find the area of the region bounded by the curve  $y = x^3$  the line  $y = 8$  and the  $y$  axis (do this in 2 different ways)
- Write down an expression for the area bounded by the  $x$  axis and the curve  $y = x^2 - x - 2 = 0$  between  $0 \leq x \leq 4$ .

