**DIFFERENTIATING GENERAL LOGARITHMIC FUNCTIONS**: In general, the derivative of a logarithmic function is given by:

$$\frac{d}{dx}(\log_a x) = \frac{1}{x \ln a}$$
$$\frac{d}{dx}(\log_a f(x)) = \frac{f'(x)}{(\ln a)f(x)}$$

Recall that differentiating the natural log function gives:

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

Hence notice that  $\ln x$  is a specific case of the general form  $\log x$  where the base is *e*. Since  $\ln(e) = 1$ , we get the same result.

Remember that product, quotient and chain rule Common question types: also apply to logarithmic functions. d

Product Rule: 
$$\frac{d}{dx}[f(x)g(x)] = f'(x)g(x) + f(x)g'(x)$$
Quotient Rule: 
$$\frac{d}{dx}\left[\frac{f(x)}{g(x)}\right] = \frac{g(x)f'(x) - f(x)g'(x)}{[g(x)]^2}$$
Chain Rule: 
$$\frac{d}{dx}[f(g(x))] = f'(g(x))g'(x)$$
1. 
$$\frac{d}{dx}A \log_a x = \frac{x \ln a}{x \ln a}$$
2. 
$$\frac{d}{dx}A \log_a Bx = \frac{A}{x \ln a}$$
3. 
$$\frac{d}{dx}A \log_a f(x) = \frac{Af'(x)}{f(x) \ln a}$$
4. 
$$\frac{d}{dx}f(x) \log_a x = f'(x) \log_a x + \frac{f(x)}{x \ln a}$$

6.1 WORKED EXAMPLE

Differentiate  $\log_2 x$  with respect to x:

6.2 WORKED EXAMPLE

Differentiate  $\log_5(x^5 + 7x^2)$  with respect to *x*: